

$$x(-x^2 - y + 3)y$$

Derivate parziali

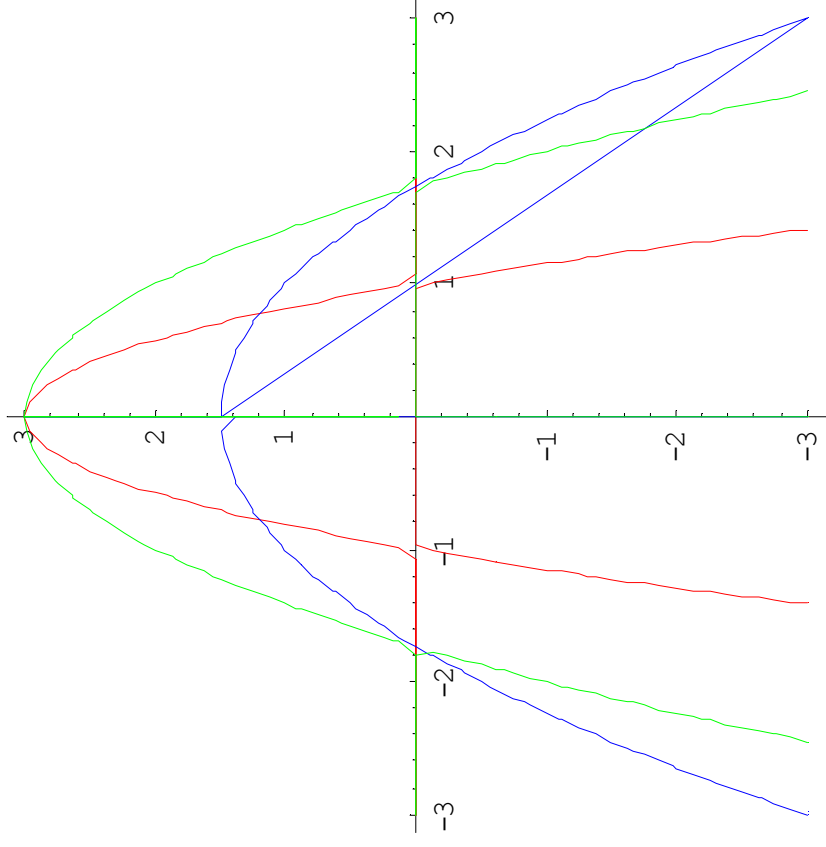
$$-y(3x^2 + y - 3)$$

$$-x(x^2 + 2y - 3)$$

Hessiano

$$\begin{pmatrix} -6xy & -3x^2 - 2y + 3 \\ -3x^2 - 2y + 3 & -2x \end{pmatrix}$$

$$\left(\begin{array}{ll} \text{sella} & \{0, 0\} & 0 & \begin{pmatrix} 0 & 3 \\ 3 & 0 \end{pmatrix} & -9 \\ \text{sella} & \{-\sqrt{3}, 0\} & 0 & \begin{pmatrix} 0 & -6 \\ -6 & 2\sqrt{3} \end{pmatrix} & -36 \\ \text{sella} & \{\sqrt{3}, 0\} & 0 & \begin{pmatrix} 0 & -6 \\ -6 & -2\sqrt{3} \end{pmatrix} & -36 \\ \text{minimo} & \left\{-\sqrt{\frac{3}{5}}, \frac{6}{5}\right\} & -\frac{36\sqrt{\frac{3}{5}}}{25} & \begin{pmatrix} \frac{36\sqrt{\frac{3}{5}}}{5} & -\frac{6}{5} \\ -\frac{6}{5} & 2\sqrt{\frac{3}{5}} \end{pmatrix} & \frac{36}{5} \\ \text{massimo} & \left\{\sqrt{\frac{3}{5}}, \frac{6}{5}\right\} & \frac{36\sqrt{\frac{3}{5}}}{25} & \begin{pmatrix} -\frac{36\sqrt{\frac{3}{5}}}{5} & -\frac{6}{5} \\ -\frac{6}{5} & -2\sqrt{\frac{3}{5}} \end{pmatrix} & \frac{36}{5} \\ \text{sella} & \{0, 3\} & 0 & \begin{pmatrix} 0 & -3 \\ -3 & 0 \end{pmatrix} & -9 \end{array} \right)$$



$$xy(-x^2 + y + 4)$$

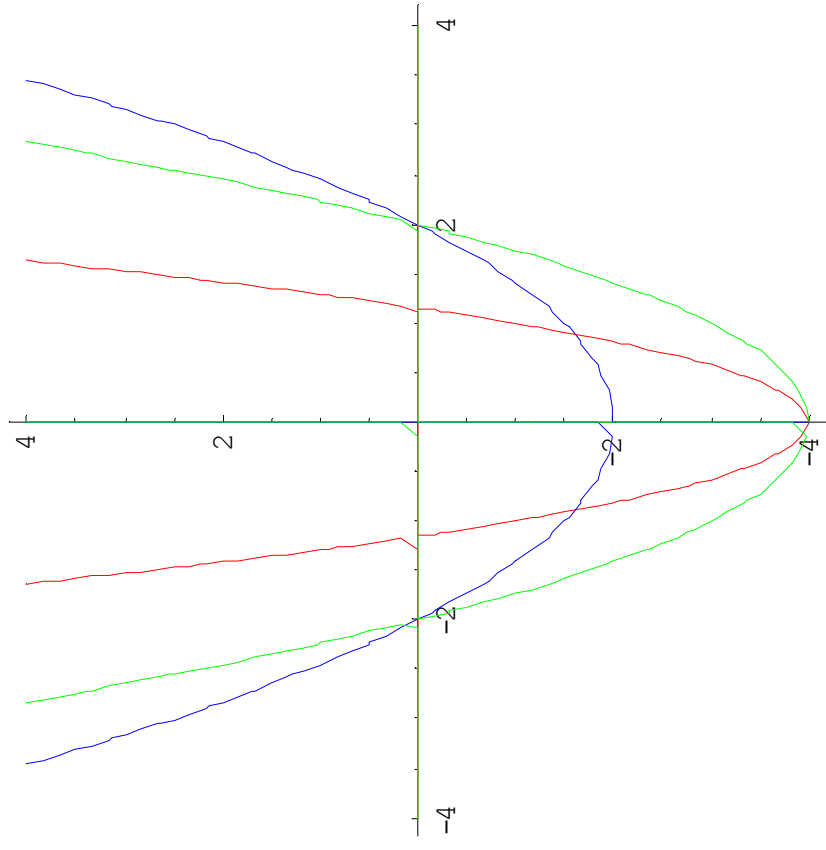
Derivate parziali

$$y(-3x^2 + y + 4)$$

$$-x(x^2 - 2y - 4)$$

Hessiano

$$\begin{pmatrix} -6xy & -3x^2 + 2y + 4 \\ -3x^2 + 2y + 4 & 2x \end{pmatrix}$$



$$\left(\begin{array}{ll} \text{sella} & \{0, 0\} & 0 & \begin{pmatrix} 0 & 4 \\ 4 & 0 \end{pmatrix} & -16 \\ \text{sella} & \{0, -4\} & 0 & \begin{pmatrix} 0 & -4 \\ -4 & 0 \end{pmatrix} & -16 \\ \text{massimo} & \left\{-\frac{2}{\sqrt{5}}, -\frac{8}{5}\right\} & \frac{128}{25\sqrt{5}} & \begin{pmatrix} -\frac{96}{5\sqrt{5}} & -\frac{8}{5} \\ -\frac{8}{5} & -\frac{4}{\sqrt{5}} \end{pmatrix} & \frac{64}{5} \\ \text{minimo} & \left\{\frac{2}{\sqrt{5}}, -\frac{8}{5}\right\} & -\frac{128}{25\sqrt{5}} & \begin{pmatrix} \frac{96}{5\sqrt{5}} & -\frac{8}{5} \\ -\frac{8}{5} & \frac{4}{\sqrt{5}} \end{pmatrix} & \frac{64}{5} \\ \text{sella} & \{-2, 0\} & 0 & \begin{pmatrix} 0 & -8 \\ -8 & -4 \end{pmatrix} & -64 \\ \text{sella} & \{2, 0\} & 0 & \begin{pmatrix} 0 & -8 \\ -8 & 4 \end{pmatrix} & -64 \end{array} \right)$$

$$(x + y)(y^2 - x)$$

Derivate parziali

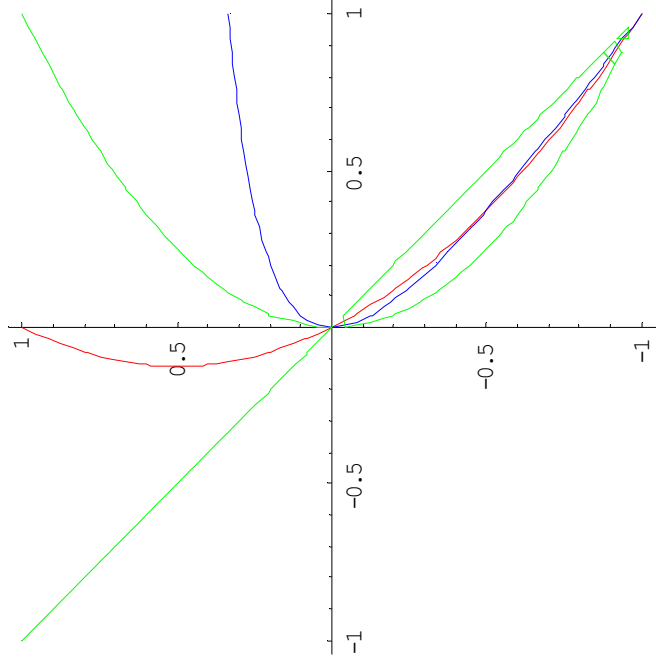
$$y^2 - y - 2x$$

$$3y^2 + 2xy - x$$

Hessiano

$$\begin{pmatrix} -2 & 2y - 1 \\ 2y - 1 & 4y + 2(x + y) \end{pmatrix}$$

$$\begin{pmatrix} \text{sella} & \{0, 0\} & 0 & \begin{pmatrix} -2 & -1 \\ -1 & 0 \end{pmatrix} & -1 \\ \text{massimo} & \left\{ \frac{3}{8}, -\frac{1}{2} \right\} & \frac{1}{64} & \begin{pmatrix} -2 & -2 \\ -2 & -\frac{9}{4} \end{pmatrix} & \frac{1}{2} \\ \text{sella} & \{1, -1\} & 0 & \begin{pmatrix} -2 & -3 \\ -3 & -4 \end{pmatrix} & -1 \end{pmatrix}$$



$$(x - y)(y - 4)(x + y - 2)$$

Derivate parziali

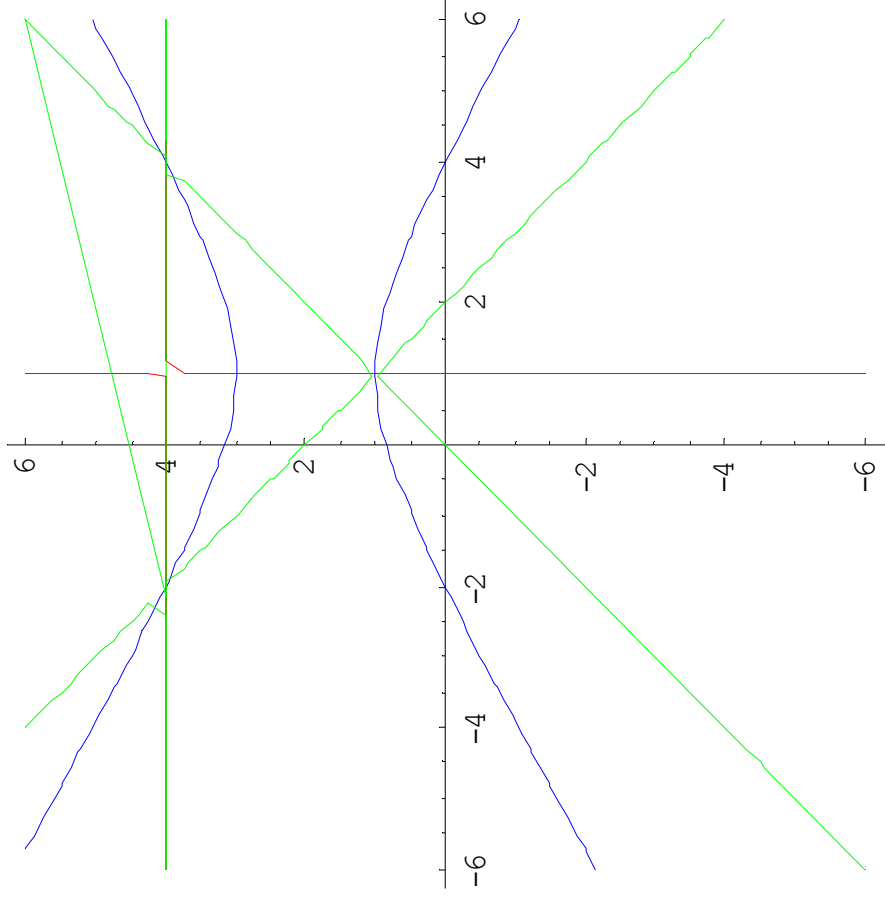
$$2(x - 1)(y - 4)$$

$$x^2 - 2x - 3y^2 + 12y - 8$$

Hessiano

$$\begin{pmatrix} 2(y - 4) & 2x - 2 \\ 2x - 2 & 2(x + y - 2) \end{pmatrix}$$

$$\begin{pmatrix} \text{sella} & \{-2, 4\} & 0 & \begin{pmatrix} 0 & -6 \\ -6 & -12 \end{pmatrix} & -36 \\ \text{sella} & \{4, 4\} & 0 & \begin{pmatrix} 0 & 6 \\ 6 & -12 \end{pmatrix} & -36 \\ \text{sella} & \{1, 1\} & 0 & \begin{pmatrix} -6 & 0 \\ 0 & 6 \end{pmatrix} & -36 \\ \text{massimo} & \{1, 3\} & 4 & \begin{pmatrix} -2 & 0 \\ 0 & -6 \end{pmatrix} & 12 \end{pmatrix}$$



$$x^2 (-x - y + 3) y^2$$

Derivate parziali

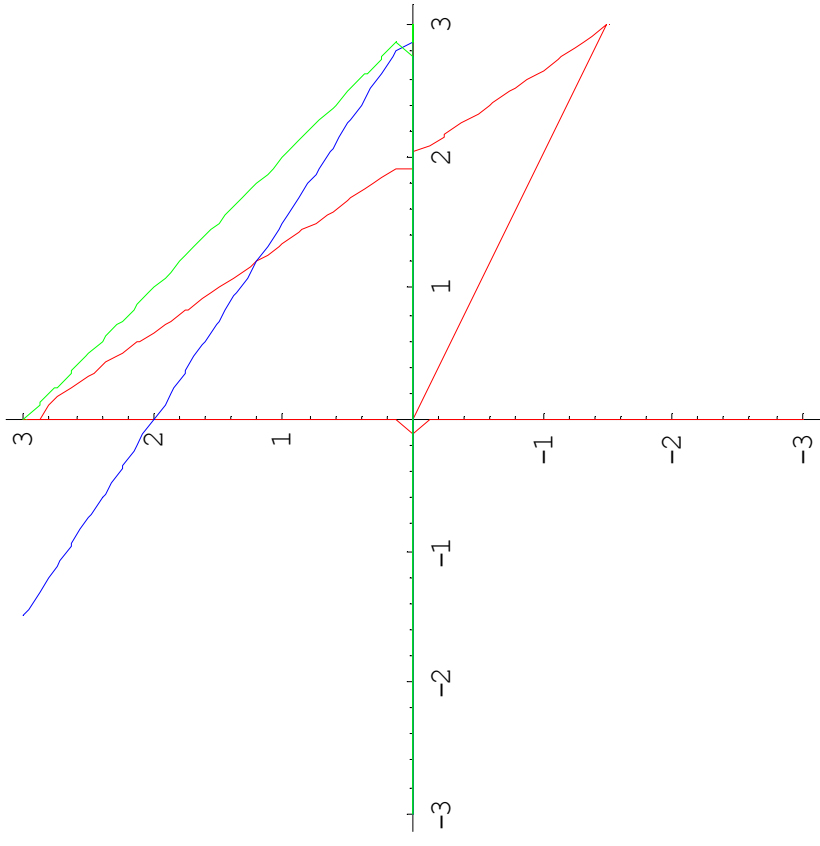
$$-x y^2 (3x + 2y - 6)$$

$$-x^2 y (2x + 3y - 6)$$

Hessiano

$$\begin{pmatrix} -2y^3 - 6xy^2 + 6y^2 & -6yx^2 - 6y^2x + 12yx \\ -6yx^2 - 6y^2x + 12yx & -2x^3 - 6yx^2 + 6x^2 \end{pmatrix}$$

$$\left(\text{massimo} \left\{ \frac{6}{5}, \frac{6}{5} \right\} \frac{3888}{3125} \begin{pmatrix} -\frac{648}{125} & -\frac{432}{125} \\ -\frac{432}{125} & -\frac{648}{125} \end{pmatrix} \frac{46656}{3125} \right)$$



$$x^2 + y^2 + \frac{1}{x+y}$$

Derivate parziali

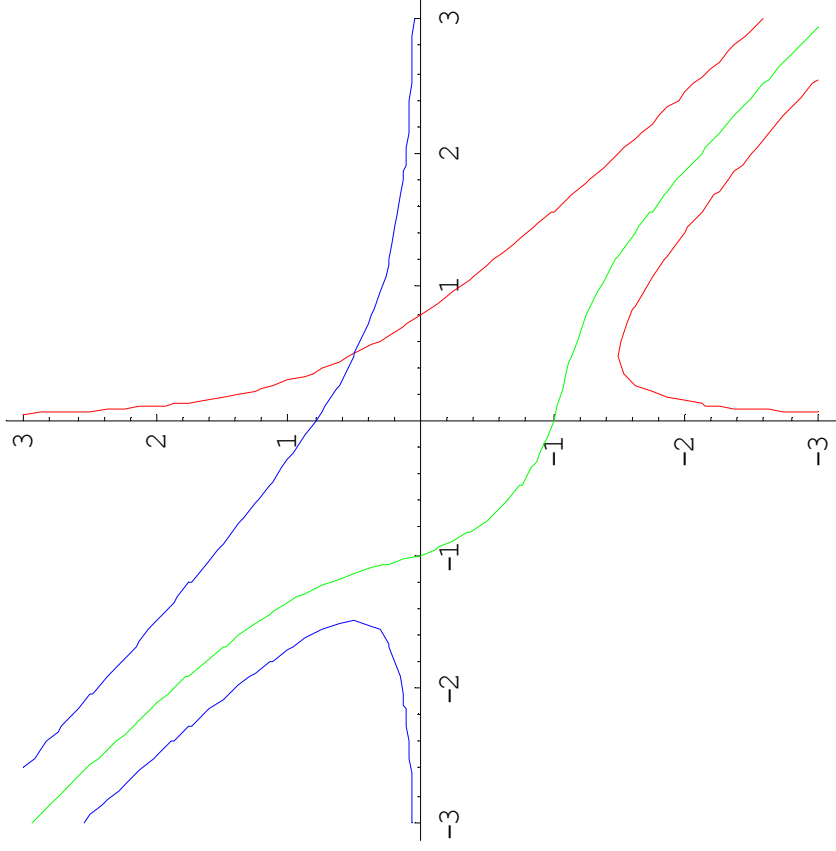
$$\frac{2x^3 + 4xy^2 + 2y^2x - 1}{(x+y)^2}$$

$$\frac{2y^3 + 4xy^2 + 2x^2y - 1}{(x+y)^2}$$

Hessiano

$$\begin{pmatrix} 2 + \frac{2}{(x+y)^3} & \frac{2}{(x+y)^3} \\ \frac{2}{(x+y)^3} & 2 + \frac{2}{(x+y)^3} \end{pmatrix}$$

$$(\text{minimo } \left\{ \frac{1}{2}, \frac{1}{2} \right\} \frac{3}{2} \begin{pmatrix} 4 & 2 \\ 2 & 4 \end{pmatrix} 12)$$



$$x^2 + 2y + \frac{1}{x+y}$$

Derivate parziali

$$2x^3 + 4yx^2 + 2y^2x - 1$$

$$(x+y)^2$$

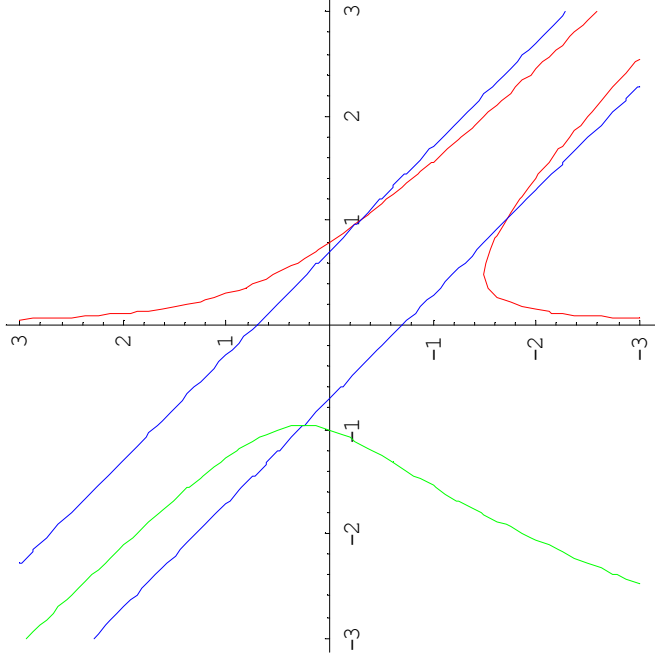
$$2x^2 + 4yx + 2y^2 - 1$$

$$(x+y)^2$$

Hessiano

$$\begin{pmatrix} 2 + \frac{2}{(x+y)^3} & \frac{2}{(x+y)^3} \\ \frac{2}{(x+y)^3} & \frac{2}{(x+y)^3} \end{pmatrix}$$

$$\begin{pmatrix} \text{sella} & \left\{ 1, \frac{1}{2}(-2 - \sqrt{2}) \right\} & -1 - 2\sqrt{2} \\ \text{minimo} & \left\{ 1, \frac{1}{2}(-2 + \sqrt{2}) \right\} & -1 + 2\sqrt{2} \end{pmatrix} \begin{pmatrix} 2 - 4\sqrt{2} & -4\sqrt{2} \\ -4\sqrt{2} & -4\sqrt{2} \end{pmatrix} \begin{pmatrix} -8\sqrt{2} \\ 8\sqrt{2} \end{pmatrix}$$



$$x y (-x^2 - y^2 + 1)$$

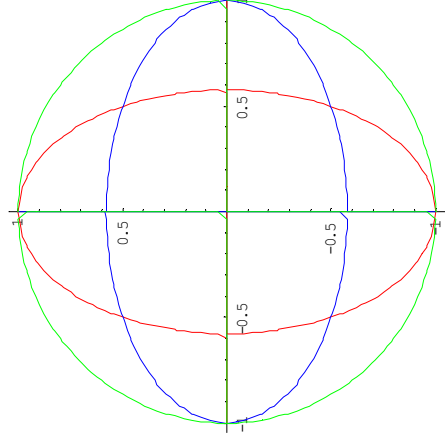
Derivate parziali

$$-y (3x^2 + y^2 - 1)$$

$$-x (x^2 + 3y^2 - 1)$$

Hessiano

$$\begin{pmatrix} -6xy & -3x^2 - 3y^2 + 1 \\ -3x^2 - 3y^2 + 1 & -6xy \end{pmatrix}$$



$$x y (-x^2 + x - y^2)$$

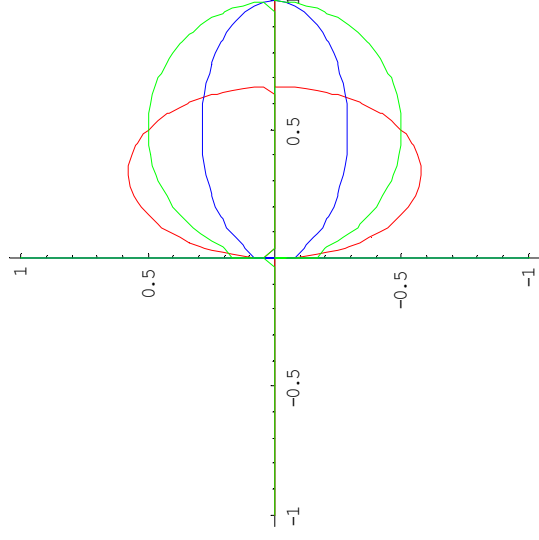
Derivate parziali

$$-y (3x^2 - 2x + y^2)$$

$$-x (x^2 - x + 3y^2)$$

Hessiano

$$\begin{pmatrix} 2y - 6xy & -3x^2 + 2x - 3y^2 \\ -3x^2 + 2x - 3y^2 & -6xy \end{pmatrix}$$



$$(x^2 - 1)(x - y^2)$$

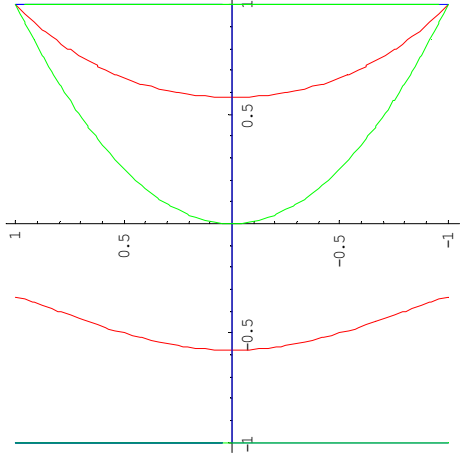
Derivate parziali

$$3x^2 - 2y^2x - 1$$

$$-2(x - 1)(x + 1)y$$

Hessiano

$$\begin{pmatrix} 6x - 2y^2 & -4xy \\ -4xy & 2 - 2x^2 \end{pmatrix}$$



$$(x^2 - x)(y - y^2)$$

Derivate parziali

$$-(2x - 1)(y - 1)y$$

$$-(x - 1)x(2y - 1)$$

Hessiano

$$\begin{pmatrix} 2y - 2y^2 & -4yx + 2x + 2y - 1 \\ -4yx + 2x + 2y - 1 & 2x - 2x^2 \end{pmatrix}$$

