

# Equazioni fratte parametriche

fra parentesi graffe i valori del parametro per i quali l'equazione è impossibile o indeterminata

- |       |  |                                      |   |
|-------|--|--------------------------------------|---|
| i.    | $\frac{x+6}{x+6-m} = \frac{x-2m+5}{x-4m+6}$      | $x = \frac{-2m^2 - 7m + 6}{m-1}$     | $\{0, \frac{1}{2}, 1\}$                         |
| ii.   | $\frac{x+2}{x+a+2} = \frac{2+x}{x+6a-5}$         | $x = -2$                             | $\{0, \frac{7}{6}\}$                            |
| iii.  | $\frac{x+6}{x-a+6} = \frac{x-2a+6}{x-4a-1}$      | $x = -\frac{2(a^2 + 3a + 21)}{a+7}$  | $\{-7, -\frac{7}{2}, -\frac{7}{3}, 0\}$         |
| iv.   | $\frac{x+1}{m+x+1} = \frac{-8m+x+1}{6m+x-3}$     | $x = \frac{-8m^2 - 13m + 4}{13m-4}$  | $\{0, \frac{2}{7}, \frac{4}{13}, \frac{4}{5}\}$ |
| v.    | $\frac{x-9k+4}{k+x+4} = \frac{x+4k+4}{6k+x-1}$   | $x = \frac{-58k^2 + 13k - 20}{8k+5}$ | $\{-\frac{5}{8}, 0, 1, \frac{5}{2}\}$           |
| vi.   | $\frac{x-9c+3}{c+x+3} = \frac{4c+x+3}{6c+x-3}$   | $x = \frac{-29c^2 + 15c - 9}{4c+3}$  | $\{-\frac{3}{4}, 0, \frac{6}{5}, 3\}$           |
| vii.  | $\frac{x-k-2}{x-5k-2} = \frac{x-4k-1}{-7k+x-2}$  | $x = \frac{13k^2 - 3k - 2}{k-1}$     | $\{-\frac{1}{3}, 0, 1\}$                        |
| viii. | $\frac{-3a+x-3}{a+x-3} = \frac{-4a+x-1}{7a+x-3}$ | $x = \frac{17a^2 + 23a - 6}{7a-2}$   | $\{0, \frac{2}{11}, \frac{2}{7}\}$              |
| ix.   | $\frac{-3a+x-2}{a+x-2} = \frac{-4a+x-1}{7a+x-2}$ | $x = \frac{17a^2 + 15a - 2}{7a-1}$   | $\{0, \frac{1}{11}, \frac{1}{7}\}$              |
| x.    | $\frac{x+9}{-a+x+9} = \frac{-2a+x-1}{x+9}$       | $x = \frac{2a^2 - 17a - 90}{3a+10}$  | $\{-5, -\frac{10}{3}, 0\}$                      |
| xi.   | $\frac{x+9}{-c+x+9} = \frac{-c+x-1}{x+9}$        | $x = \frac{c^2 - 8c - 90}{2(c+5)}$   | $\{-10, -5, 0\}$                                |
| xii.  | $\frac{-2k+x+9}{-k+x+9} = \frac{-k+x-1}{x+9}$    | $x = \frac{1}{10}(k^2 + 10k - 90)$   | $\{-10, 0\}$                                    |
| xiii. | $\frac{-2m+x+5}{-m+x+5} = \frac{x-5}{-2m+x+5}$   | $x = \frac{4m^2 - 25m + 50}{3m-10}$  | $\{0, \frac{10}{3}, 5\}$                        |
| xiv.  | $\frac{3k+x+5}{-k+x+5} = \frac{-k+x-2}{x+5}$     | $x = \frac{k^2 - 18k - 35}{5k+7}$    | $\{-7, -\frac{7}{5}, 0\}$                       |
| xv.   | $\frac{x+1}{-b+x+1} = \frac{-b+x-2}{x+1}$        | $x = \frac{b^2 + b - 3}{2b+3}$       | $\{-3, -\frac{3}{2}, 0\}$                       |
| xvi.  | $\frac{x+3}{-a+x+3} = \frac{x-4a}{x+3}$          | $x = \frac{4a^2 - 12a - 9}{5a+3}$    | $\{-\frac{3}{4}, -\frac{3}{5}, 0\}$             |

xvii.	$\frac{x^2 - (2+k)x + 1+k}{x+2k-1} = x-2-k$	$x = \frac{6k-1}{3k-1}$	$\left\{-\frac{1}{6}, 0, \frac{1}{3}\right\}$
xviii.	$\frac{2x+5a+1}{1-a-x} = a+2$	$x = \frac{1-6a-a^2}{a+4}$	$\{-4, -1\}$
xix.	$\frac{x-3k}{x+2k+5} = 2k+1$	$x = -\frac{4k^2+15k+5}{2k}$	$\{-1, 0\}$
xx.	$\frac{2x+a+b}{x-a+b} = a-2b$	$x = \frac{3ab-a-b-a^2-2b^2}{2-a+2b}$	$\{a=2+2b, b=3a\}$
xxi.	$\frac{x+3-k}{x-2k+1} = 3-k$	$x = \frac{2k(k-3)}{k-2}$	$\{-2, 2\}$
xxii.	$\frac{2x+3k}{x-k+1} = k-3$	$x = \frac{k^2-k+3}{k-5}$	$\left\{\frac{2}{5}, 5\right\}$
xxiii.	$\frac{x-2a}{x+a+1} = 2a$	$x = \frac{2a^2}{1-2a}$	$\left\{\frac{1}{3}, \frac{1}{2}\right\}$
xxiv.	$\frac{5-3x}{1+k-x} = k+1$	$x = \frac{k^2+2k-4}{k-2}$	$\{-2, 2\}$
xxv.	$\frac{x-a-b}{x-a-2b} = \frac{x-2a+b}{x-2a}$	se $b=0$ $x \neq a \wedge x \neq 2a$	
xxvi.	$\frac{x^2-10x-kx+25+5k-2k^2}{x-5} = x-2-k$	$x = \frac{15-2k^2}{3}$	$\{0\}$
xxvii.	$\frac{x^2-2ax+a^2-b^2}{x-a-2b} = x-3a$	$x = \frac{2a^2+b^2+6ab}{2a+2b}$	$\{b=0\}$
xxviii.	$\frac{x-2}{x-2+k} = \frac{x+5-2k}{x+5-3k}$	$x = \frac{2k-3}{2}$	$\left\{\frac{3}{8}, \frac{7}{4}\right\}$
xxix.	$\frac{x-6+k}{x+2k-6} = \frac{x+2k+2}{x-6}$	$x = \frac{2(2k^2-k-24)}{3k+8}$	$\{-4, 0\}$
xxx.	$\frac{x+3k}{x-5k} = \frac{x+2}{x-k+2}$	$x = \frac{3k-16}{7}$	$\left\{se\ k=0 \forall x \neq 0 \wedge x \neq -2, -\frac{1}{2}\right\}$
xxxi.	$\frac{x-1+2k}{x-1+k} = \frac{x+2}{x-1}$	$x = \frac{4k-3}{k-3}$	$\{0, 3\}$
xxxii.	$\frac{2kx+1}{x-2k} = \frac{k}{k^2+1}$	$x = -\frac{1}{k}$	$\{0\}$
xxxiii.	$\frac{x+5a+2}{x-6a+3} = \frac{6a+1}{2-5a}$	$x = a-1$	$\left\{\frac{1}{11}, \frac{2}{5}\right\}$
xxxiv.	$\frac{x+m+1}{x+m} = 1 + \frac{1}{m}$	$x = 0$	

xxxv.	$\frac{bx+2}{1-bx+3b} = \frac{1}{b}$	$x = 1/b$	
xxxvi.	$\frac{nx+n+1}{3nx+2} = \frac{n+3}{8}$	$x = \frac{2}{n}$	
xxxvii.	$\frac{x+3p}{x-1} = 1-p-3p^2$	$x = 1 - \frac{1}{p}$	$\left\{-\frac{1}{3}\right\}$
xxxviii.	$\frac{r-x}{1+2x} = \frac{r^2-r+3}{3r-6}$	$x = \frac{r-3}{r}$	
xxxix.	$\frac{x+2}{x+u} = \frac{2u+1}{3u-1}$	$x = 2u-1$	$\left\{\frac{1}{3}, 2\right\}$
xl.	$\frac{x+v+1}{x+2v-2} = \frac{v^2+2v-1}{2v^2-v-1}$	$x = \frac{v-1}{v}$	$\left\{-\frac{1}{2}, 1, 3\right\}$
xli.	$\frac{2x-h}{3x-h+1} = \frac{h-6}{2h-8}$	$x = h-3$	
xlii.	$\frac{x+a^2}{x+a^2-2a} = a+1$	$x = 2+2a-a^2$	
xliii.	$\frac{x+2}{x-c+1} = c^2-c$	$x = \frac{c^3-2c^2+c-2}{c^2-c-1}$	$\{-1\}$
xliv.	$\frac{x-2q}{x-1+q} = q^2$	$x = \frac{q(q-2)}{1-q}$	$\{-1, 1\}$
xliv.	$\frac{x+1-s}{x+s} = 1-s^2$	$x = \frac{-s^3+2s-1}{s^2}$	$\left\{0, \frac{1}{2}\right\}$